# Modeling an Integrated Multi-Distributor Supply Chain with Production Mean

by

M. Abolhasanpour<sup>1</sup>, A.M. Kimiagari<sup>2</sup>, A. Abolhasanpoor<sup>3</sup>, M. Tajalli, F<sup>4</sup>, Vaezi Shokouh<sup>5</sup> <sup>1,2</sup>Department of Industrial Engineering, Amirkabir University of Technology, Iran <sup>3,4</sup>Asia Pacific International College, Australia <sup>5</sup>Mehr Alborz Nonprofit Institution, Iran E-mail: m.abolhasanpour@gmail.com

## Abstract

One of the most important challenges in a Single-Vendor multiple-Distributor Multiple-Buyers supply chain is deciding about production mean amount. Production mean determines yield rate of the vendor that could affect production lot size and specify number of shipments between vendor, distributor and buyers. In this paper, an integrated Single-Vendor multiple-Distributor Multiple-branch problem formulated. In this model vendor allowed to deliver product lots to distributor in an unequal-sized shipments manner. Respectively distributor has been allowed to deliver products to each customer base on its demand. Outgoing items will be inspected and will be reprocessed if couldn't satisfy lower specification limits. This model expected to lower reprocessing cost due to the deviation from the optimum target value. Because of nonlinearity that exists on the total cost function due to fraction of conforming items produced and also ratio of yield rate to demand rate, we suggested a step by step numerical solution algorithm to finding the model optimal solution.

**Keywords:** Supply Base Supply Chain, Integrated Model, Heuristic Solution, Production Mean, Numerical Solution

## **1. Introduction**

Eliminating all of the production variations is not possible but quality control procedures are effective in order to decreasing products variation (Montgomery, 2005)[1]. In the literature so many tools used to decrease variation in a production process. Targeting that particularly utilized in container-filling processes is one of them (i.e., cosmetic, drug, and health-care industries) (Duffuaa and Siddiqui, 2003)[2]. Containers, in like this processes, are filled with materials base on lower specification limits (Roan et al., 2000)[3]. However, there is a trade-off between expenses of a very tight process specifications and products reprocessing (Al-Sultan and Pulak, 2000)[4]. Recently, researchers formulated numbers of analytical models that combines targeting with inventory or production problems (Gong et al., 1988[3]; Al-Fawzan and Hariga, 2002[5]; Williams et al., 2000 [6]; Hariga and Al-Fawzan, 2005[32]). Supply chain management development force firms to concentrate on managing inventories over entire supply chain (Ben-Daya et al., 2008[9]). In the literature, the single-vendor single-buyer

problem as the building block of the wider supply chain models studied but there is not any special direction to multiple-buyer state of the supply chain problem

In this model vendor allowed to deliver product lots to distributor in an unequal-sized shipments manner. Respectively distributor has been allowed to deliver products to each customer base on its demand. Outgoing items will be inspected and will be reprocessed if couldn't satisfy lower specification limits. Literature review discussed in the next section. The notation, problem statement and assumptions introduced in Sections 3 and 4, respectively. In Section 5, modeling framework is presented. Vendor-distributor-buyer models are developed in Section 6. In Section 7, solution procedure illustrated and finally section 8 concludes the paper.

## 2. Notation

The following notation has been used in developing the proposed model:

- D demand rate
- production rate
- $\hat{W}$  distributors warehouse rate
- X a random variable represents the amount of raw material an item receives
- *L* lower specification limit
- **P** fraction of conforming items produced
- $\lambda$  yield rate of process  $(\lambda = rp)$
- P ratio of yield rate to demand rate (P = k/D)
- Ň number of corporate branches
- D number of corporate distributors
- $A_v$  vendor setup cost
- A<sub>u</sub> distributor ordering cost
- *A*<sup>b</sup> branches ordering cost
- Ar ordering cost of raw material
- $h_{\mathcal{V}}$  holding cost for the vendor per item per unit time
- $\mathbf{h}_{d}$  holding cost for the distributor per item per unit time
- **h**<sub>b</sub> holding cost for the buyer per item per unit time
- $\mathbf{h}_{\mathbf{r}}$  holding cost for the raw material per unit per unit time
- **R** per-item reprocessing cost
- b fixed production cost (b > 0)
- $\alpha$  value-added factor ( $\alpha \ge 1$ )
- C unit material cost
- q<sub>i</sub> size of th shipment
- Q production lot size
- T inventory cycle length (T = 🐴
- N number of cycles  $(N = \frac{1}{2})$
- n number of shipments

 $T_p$  production cycle length ( $T_p = Q/\lambda$ )  $TC_1$  average total cost per unit time when D = W  $TC_2$  average total cost per unit time when D > W  $TC_3$  average total cost per unit time when D < W  $\varepsilon$  demand rate probability when P(D = W)  $\beta$  demand rate probability when P(D < W)  $\gamma$  demand rate probability when P(D > W) $\Phi$  back order cost per item per unit time

### 3. Problem Statement and Assumptions

In this model vendor orders raw materials from supplier and uses in lots of Q. X represents the amount of raw material that an item receives. L represents lower specification limit. X considers to be better whenever it is greater. Each item categorized as standard if X is greater or equal to L. Otherwise it requires reprocessing operation. Performance variable X according what that stated by M.A. Darwish(2009)[37] assumed to have a normal distribution function with mean  $\mu$  and constant variance  $\sigma^2$ .  $\Phi$  represents standard normal distribution density function of conforming items.

$$p = P[X \ge L] = P\left[Z \ge \frac{L-\mu}{\sigma}\right] = \int_{\frac{L-\mu}{\sigma}}^{\infty} \Phi(z) dz$$

Production rate is r and production yield rate is  $\lambda = rp$ . Raw materials inventory is increased by the sum of recovered raw material  $r(1-p) T_p$  and the amount of raw material that vendor receives from supplier  $r(\mu - (1-p)) T_p$ . The shipment policy that developed by Goyal(1995) has been used in this model. Base on this policy, n unequal-sized shipments delivers to distributor. Size of *i*th shipment ( $\mathbf{q}_i$ ) is equal to

$$q_{i} = q_{i-1} \left(\frac{\lambda}{D}\right), i = 2, 3, \dots, n.$$

$$q_{i} = q_{1} \left(\frac{\lambda}{D}\right)^{i-1}, i = 2, 3, \dots, n.$$

$$Q = \sum_{i=1}^{n} q_{i} = q_{1} \frac{\rho^{n} - 1}{\rho - 1}$$

The inventory cycle length is :  $T = \frac{q_{\perp} \rho^n - 1}{p_{\perp} \rho - 1}$  and  $\rho = \lambda/D$ 

## 4. Modeling Framework

The costs in this model include vendor, distributor, inventory control of raw material, production and also customer loss costs. These costs described as bellows:

## 4.1 Corporate branches costs

Branches incur ordering and holding costs. Shipment takes time  $Q_t/D$  per time and in this time branche's average inventory is  $Q_t/2$ . Average inventory per cycle =  $\sum_{k=1}^{n} Q_t^2/2D$ Average cost of branch inventory per cycle =  $HC_b = h_b \sum_{k=1}^{n} \frac{Q_t^2}{2D} = \frac{h_b Q_b}{2D} \frac{e^{5n} - 1}{e^{5} - 1}$ Average total cost of the branches per unit time =  $\check{N}(\frac{nA_b + HC_b}{7}) = \check{N}(\frac{nA_b D}{Q_b} \frac{e^{-1}}{e^{1} - 1} + \frac{h_b Q_b e^{n}}{2} \frac{e^{n} + 1}{e^{1} - 1})$ 

## 4.2 Vendor's costs

Vendor also has setup and holding costs. For each production run vendor has setup cost  $A_{u}$ . As stated by Darwish(2009)[37] vendor costs is as belows:

Average vendor inventory cost per cycle =  $RC_{\nu} = h_{\nu} \sum_{i=1}^{n} \frac{q_{i}}{2i} = \frac{h_{\nu}q_{\nu}}{2i} \frac{p^{n}-1}{p^{n}-1}$ Average vendor total cost per unit time =  $C_{\nu} = \left(\frac{A_{\nu}D}{q_{\nu}} \frac{p^{-1}}{p^{n}-1} + \frac{h_{\nu}q_{\nu}}{2p} \frac{p^{n}+1}{p^{n}+1}\right)$ 

## 4.3 Inventory control costs related to raw materials

Inventory control costs related to raw materials includes ordering cost and holding cost also. Like what that stated by M.A. Darwish(2009) [37] Average total cost of inventory control of raw materials =  $Q_p = \frac{1}{Q_p} \frac{p-1}{p^n-1} (A_p + \frac{h_p}{p_p} Q^2)$ 

#### 4.4 Direct production costs

We assumed that direct production cost is a linear function and exactly like what that stated by M.A. Darwish [37] it is as below:

Per cycle cost of producing Q items =  $r \int_{0}^{\tau_{F}} g(\mu) dt$ 

Reprocessing cost of per item = R

Reprocessing cost of items in per cycle = R(1 - p).r.T<sub>p</sub>

Amount of raw materials in vendors warehouse at = 0:  $I_{\mu}(0)$ 

Amount of raw materials that vendor receives from supplier in one cycle =  $I_p(0) - r(1-p)T_p$ 

Raw material acquisition cost per cycle =  $C - C(I_p(0) - r(1-p)|T_p|) = \frac{c_q}{p}(\mu - (1-p))$ Total production cost per unit time =  $C_p = \frac{p}{q_1} \frac{p-1}{p^n-1} \left( \frac{(b+c((a+1)\mu - (1-p)))}{p} Q + \frac{1-p}{p} RQ \right)$ 

#### 4.5 Distributor costs

The distributors cost consists of inventory holding cost, ordering cost, customer loss costs. Distributor output rate  $(\hat{W})$  assumed to be a linear function of production rate and directly depends to vendor's output. Customer demand has three statuses as below:

- 1.  $P(D = W) = \varepsilon$
- 2.  $P(D \prec W) = \beta$
- 3.  $P(D > W) = \gamma$

While:  $0 \le \varepsilon$ ,  $\beta$ ,  $\gamma \le 1$  and  $\varepsilon + \beta + \gamma = 1$ . In each of these three different customer demand statuses, distributors have different type of costs that it takes into study next.

5.5.1. Average total cost of the distributors per unit time =  $D\left(\frac{M}{T}\right)$ ,  $P(D = W) = \varepsilon$ 

5.5.2. Average total cost of the distributors per unit time =  $D\left(\frac{nd_d}{T}\right) + \Phi\left(\frac{p}{N} - \begin{pmatrix} q_1^2 \\ 2D \end{pmatrix}\right)$ ,  $P(D < W) = \beta$ 5.5.3. Average demand from distributor in each cycle =  $\frac{p}{N}$ Average distributor inventory per cycle =  $\sum_{i=1}^{n} \frac{q_i^2}{2D}$ Average cost of distributor inventory per cycle =  $HC_d = h_d\left(\frac{p}{N} - \sum_{i=1}^{n} \frac{q_i^2}{2D}\right) = h_d\frac{p}{N} - h_d\frac{q_u^2}{2D}\frac{p^{2n} - 1}{p^2 - 1}$ Distributor ordering cost per cycle = n.  $A_d$ Average total cost of the distributors per unit time =  $D\left(\frac{md_d + \left(h_d\frac{p}{N} - h_d\frac{q_u^2}{2D}\frac{p^{2n} - 1}{p^2 - 1}\right)}{T}\right)$ ,  $P(D > W) = \gamma$ 

## 5. Total Cost Function

According what that stated before on section 5, state based customers demand lead to a state based total cost function that each cost function could be formulated as below.

$$\begin{split} TC_{1} &= \check{N} \left( \frac{nA_{2}D}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{5}q_{4}}{2} \frac{\rho^{n}+1}{\rho+1} \right) + \left( \frac{A_{2}h}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{4}}{2\rho} \frac{\rho^{n}+1}{\rho+1} \right) + \frac{h}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} \left( A_{p} + \frac{h_{p}\mu}{2rp^{2}} Q^{2} \right) + \frac{p}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} \left( \frac{(b+c((a+1)\mu-(1-p)))}{p} Q + \frac{1-p}{p} RQ \right) + D\left( \frac{NA_{4}}{T} \right) \\ TC_{2} &= \check{N} \left( \frac{uA_{2}D}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{5}q_{4}}{2} \frac{\rho^{n}+1}{\rho+1} \right) + \left( \frac{A_{2}D}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{4}}{2\rho} \frac{\rho^{n}+1}{\rho+1} \right) + \frac{p}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} \left( A_{p} + \frac{h_{p}\mu}{2rp^{2}} Q^{2} \right) + \frac{p}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} \left( \frac{(b+c((a+1)\mu-(1-p)))}{p} Q + \frac{1-p}{p} RQ \right) + D\left( \frac{nA_{4}}{T} \right) + \Phi\left( \frac{h}{N} - \left( \frac{q_{1}^{2}}{2D} \right) \right) \\ TC_{3} &= \check{N} \left( \frac{nA_{2}D}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{4}}{2} \frac{\rho^{n}+1}{\rho+1} \right) + \left( \frac{A_{2}D}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{6}}{2\rho} \frac{\rho^{n}+1}{\rho+1} \right) + \frac{p}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} \left( A_{p} + \frac{h_{p}\mu}{2rp^{2}} Q^{2} \right) + \frac{p}{q_{4}} \frac{\rho^{-1}}{\rho^{n}-1} \left( \frac{(b+c((a+1)\mu-(1-p)))}{q_{5}} Q + \frac{1-p}{p} RQ \right) + D\left( \frac{nA_{4}}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{6}}{2\rho} \frac{\rho^{n}+1}{\rho+1} \right) + \frac{p}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} \left( A_{p} + \frac{h_{p}\mu}{2rp^{2}} Q^{2} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{n}-1} \left( \frac{(b+c((a+1)\mu-(1-p)))}{q_{5}} Q + \frac{1-p}{p} RQ \right) + D\left( \frac{nA_{4}}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{2}q_{6}}{2\rho} \frac{\rho^{n}-1}{\rho^{1}-1} \right) + \frac{p}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} \left( A_{p} + \frac{h_{p}\mu}{2rp^{2}} Q^{2} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{n}-1} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{n}-1} \left( \frac{h_{p}(a_{6})}{q_{5}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{p}(a_{6})}{\rho^{n}-1} \right) + \frac{h_{p}(a_{6})}{\rho^{n}-1} \left( \frac{h_{p}(a_{6})}{\rho^{n}} \frac{\rho^{-1}}{\rho^{n}-1} + \frac{h_{p}(a_{6})}{\rho^{n}} \frac{\rho^{-1}}{\rho^{n}-1} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{-1}} \left( \frac{h_{p}(a_{6})}{\rho^{n}} \frac{\rho^{-1}}{\rho^{n}-1} \right) + \frac{h_{p}(a_{6})}{\rho^{-1}} \frac{\rho^{-1}}{\rho^{-1}} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{-1}} \left( \frac{h_{p}(a_{6})}{\rho^{-1}} \frac{\rho^{-1}}{\rho^{-1}} \right) + \frac{p}{q_{6}} \frac{\rho^{-1}}{\rho^{-1}} \left( \frac{h_{p}(a_{6})}{\rho^{-1}} \frac{\rho^{-1}}{\rho^{-1}} \frac{\rho^{-1}}{\rho^{-1}} \right) + \frac$$

## 6. Solution Algorithm

The decision variables in this model are the production mean( $\mu$ ), number of vendor's shipments (n) and size of first shipments. We assumed that shipments are equal. The probability function for  $\varepsilon$ ,  $\beta$ and  $\gamma$  are the same and in this model we could take into study the optimistic or pessimistic customers demand rate and its effect on the entire supply chain costs by sensitivity analysis process. Note that pand  $\rho$  that used in the section 6 are not constants also but functions of the production mean ( $\mu$ ). The objective of this model is to minimize Z in which

 $Z = e TC_1 + \beta TC_2 + \gamma TC_3$  While  $e + \beta + \gamma = 1$  and  $0 \le \varepsilon$ ,  $\beta$ ,  $\gamma \le 1$ . Z is a linear function of  $TC_1$ ,  $TC_2$  and  $TC_3$  and therefore if we could prove that TC functions are convex, therefore the convexity of Z will be concluded. We can easily prove that TC functions that has been used in this model are convex functions in  $q_1$  because  $\frac{\beta \cdot TC_2}{\beta \cdot q_2}$  and  $\frac{\beta \cdot TC_2}{\beta \cdot q_2} \ge 0$ . Therefore for given values of  $e_1\beta_1\gamma$ , n and  $\mu$ , the value of  $q_1$  which minimizes Z could be obtained by differentiating Z function with respect to  $q_1$  and setting its results to 0. Then the average total cost per unit time of the integrated scenario based model (Z  $\gamma$ ) would be obtained by setting amount of  $q_1$  in the Z function. Because of nonlinearity of Z that exists due to p and p, the optimal solution could be found numerically. Steps that listed below could be use to finding an optimal solution.

Step 1: Set n = 0 and  $\mathbb{Z}_{min} \to \infty$ Step 2: Increase n by 1 Step 3: Determine the value of  $\mu$  which minimizes  $\mathbb{Z}^*$ Step 4: If  $\mathbb{Z}^* \ll \mathbb{Z}_{min}$  set  $\mathbb{Z}_{min} = \mathbb{Z}^*, n^* = n$  and  $\mu^* = \mu$ . Go to step 2. Step 5: Stop.

## 7. Conclusion

Multiple branch problem and targeting problem has been integrated in this paper. Optimal process mean, production lot size and number of deliveries regarded in this model. We assumed that demand rate of the customers are base on a status based manner. Also we assumed that distributors are isolated from each of other distributors. Because of nonlinearity that exists on the total cost function due to fraction of conforming items produced and also ratio of yield rate to demand rate, we suggested a step by step numerical solution algorithm to finding the model optimal solution. Relationship between distributors could be considered as a future study on this paper.

## References

Montgomery, D., 2005. Introduction to Statistical Quality Control, fifth ed. John Wiley & Sons.

Duffuaa, S.O., Siddiqui, A.W., 2003. Process targeting with multi-class screening and measurements error. International Journal of Production Research 41 (7), 1373–1391.

Gong, L., Roan, J., Tang, K., 1988. Process mean determination with quantity discounts in raw material cost. Decision Sciences 29 (1), 271–302.

Al-Sultan, K.S., Pulak, M.F.S., 2000. Optimum target values for two machines in series with 100% inspection. European Journal of Operational Research 120, 181–189.

Al-Fawzan, M.A., Hariga, M., 2002. An integrated inventory-targeting problem with time dependent process mean. Production Planning and Control 13 (1), 11–16.

Williams, W.W., Tang, K., Gong, L., 2000. Process improvement for a containerfilling process with random shifts. International Journal of Production Economics 66 (1), 23–31.

Goyal, S.K., 1977. Determination of optimum production quantity for a two stage system. Operational Research Quarterly 28, 865–870.

Banerjee, A., 1986. A joint economic lot size model for purchaser and vendor. Decision Sciences 17, 292–311.

Ben-Daya, M., Darwish, M., Ertogral, K., 2008. The joint economic lot sizing problem: Review and extensions. European Journal of Operational Research 185 (2), 726–742.

Goyal, S.K., 1988. A joint economic lot size model for purchaser and vendor: A comment. Decision Sciences 19, 236–241.

Goyal, S.K., 1995. A one-vendor multi-buyer integrated inventory model: A comment. European Journal of Operational Research 82, 209–210.

Hill, R.M., 1997. The single-vendor single-buyer integrated production–inventory model with a generalized policy. European Journal of Operational Research 97, 493–499.

Goyal, S.K., Nebebe, F., 2000. Determination of economic production–shipment policy for a single-vendor single-buyer system. European Journal of Operational Research 121, 175–178.

Hill, R.M., 1999. The optimal production and shipment policy for single-vendor single buyer integrated production–inventory problem. International Journal of Production Research 37 (11), 2463–2475.

Chang, H.C., Ouyang, L.Y., Wu, K.S., Ho, C., 2004. Integrated vendor-buyer cooperative inventory models with controllable lead time and ordering cost reduction. European Journal of Operational Research 170 (2), 481–495.

Pan, J.C., Yang, J.S., 2002. A study of an integrated inventory with controllable lead time. International Journal of Production Research 40 (5), 1263–1273.

Ouyang, L.Y., Wub, K.S., Hoc, C.H., 2004. Integrated vendor–buyer cooperative models with stochastic demand in controllable lead time. International Journal of Production Economics 92 (3), 255–266.

Hoque, M.A., Goyal, S.K., 2006. A heuristic solution procedure for an integrated inventory system under controllable lead-time with equal or unequal sized batch shipments between a vendor and a buyer. International Journal of Production Economics 102 (2), 217–225.

Hill, R., Omar, M., 2006. Another look at the single-vendor single-buyer integrated productioninventory problem. International Journal of Production Research 44 (4), 791–800.

Zhou, Y., Wang, S., 2007. Optimal production and shipment models for a singlevendor– single-buyer integrated system. European Journal of Operational Research 180 (1), 309–328.

Hunter, W.G., Kartha, C.P., 1977. Determining the most profitable target value for a production process. Journal of Quality Technology 9 (3), 176–181.

Bisgaard, S., Hunter, W.G., Pallesen, L., 1984. Economic selection of quality of manufactured products. Technometrics 26, 9–18.

Golhar, D.Y., 1987. Determination of the best mean contents for a canning problem. Journal of Quality Technology 19 (2), 82–84.

Golhar, D.Y., Pollock, S.M., 1988. Determination of the best mean and the upper limit for a canning problem. Journal of Quality Technology 20 (3), 188–192.

Boucher, T.O., Jafari, M., 1991. The optimum target value for single filling operations with quality sampling plans. Journal of Quality Technology 23 (1), 47–48.

Arcelus, F.J., Banerjee, P.K., 1985. Selection of the most economical production plan is a tool-wear process. Technometrics 27 (4), 433–437.

Rahim, M.A., Banerjee, P.K., 1988. Optimum production run for a process with random linear drift. Omega 16 (4), 317–351.

Al-Sultan, K.S., Al-Fawzan, M.A., 1997. An extension of Rahim and Banerjee's model for a process with upper and lower specification limits. International Journal of Production Economics 3, 265–280.

Rahim, M.A., Al-Sultan, K.S., 2000. Joint determination of the optimum target mean and variance of a process. Journal of Quality in Maintenance Engineering 6 (3), 192–199.

Shao, Y.E., Fowler, J.W., Runger, G.C., 2000. Determining the optimal target for a process with multiple markets and variable holding costs. International Journal of Production Economics 65 (3), 229–242.

Lee, M.K., Elsayed, A.E., 2002. Process mean and screening limits for filling processes under two-stage screening procedure. European Journal of Operational Research 138 (1), 118–126.

Hariga, M.A., Al-Fawzan, M.A., 2005. Joint determination of target value and production run for a process with multiple markets. International Journal of Production Economics 96 (2), 201–212.

Darwish, M.A., 2004a. Determination of the optimal process mean for a single vendor–single buyerproblem. International Journal of Operations and Quantitative Management 10 (3), 1–13.

Darwish, M.A., 2004b. An integrated single-vendor single-buyer targeting problem. In: Second International Industrial Engineering Conference, Riyadh, Saudi Arabia.

Lee, M.K., Kwon, H.M., Hong, S.H., Kim, Y.J., 2007. Determination of the optimum target value for a production process with multiple products. International Journal of Production Economics 107 (1), 173–178.

Gibra, I.N., 1974. Optimal production runs of processes subject to systematic trends. International Journal of Production Research 12 (4), 511–517.

M.A. Darwish, (2009). Economic selection of process mean for single-vendor single-buyer supply chain, European Journal of Operational Research. 199, 162–169.